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B.COM. (HONOURS) PART- III TEST EXAMINATION, 2017.
SUB.: - ADVANCED BUSINESS MATHEMATICS & STATISTICS
PAPER - VIII

F.M. -50

TIME: 2 HOURS

1. Answer any five (5) questions-

2X5=10

(a) Given $A = \begin{bmatrix} 4 & 2 & -1 \\ 3 & -7 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 3 \\ -3 & 0 \\ -1 & 5 \end{bmatrix}$, find AB.

(b) Evaluate $\lim_{x \rightarrow 2} \left(\frac{x^5 - 32}{x - 2} \right)^n$

(c) Write down 'mean' and 'variance' of a binomial distribution.

(d) Find $\frac{dy}{dx}$ when $(x^2 + y^2) = a^2$

(e) Distinguish between 'population' and 'sample'

(f) Evaluate $\int \frac{(1-x)^3}{x} dx$

(g) If $A = \{1, 3, 5, 9\}$ and $B = \{1, 2, 3, 4, 5, 6, 7, 8\}$, find $(A \cap B)$

(h) State Whether $0 \leq P(A) \leq 1$ is correct or not ;

What is the significance of $P(A) = 1$?

2. Answer any two (2) questions-

10X2=20

(a) Prove that the matrix A given by $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$

satisfies the relation $A^2 - A(a + d) + (ad - bc)I = 0$, where I is a unit matrix of order two.

(b) If $\sqrt{1 - x^2} + \sqrt{1 - y^2} = a(x - y)$, show that $\frac{dy}{dx} = \sqrt{\frac{1 - y^2}{1 - x^2}}$

(c) (i) Find the area bounded by the parabolas

$y^2 = 16x$ and $x^2 = 16y$.

(ii) Evaluate the following integrals by the method of substitution:

$$\int \frac{x^2 - 1}{x} \cdot e^x dx$$

(d) Examine the maximum and minimum of $f(x) = x^3 + 12x^2 + 36x + 8$

3. Answer any two (2) questions-

10X2=20

a. From a pack of 52 cards, 1 card is drawn at random. Find the chance of (i) drawing a spade, and (ii) not drawing a spade.

b. For any events A and B, which are not mutually exclusive, prove that

$$P(A \cup B) = P(A) + P(B) - P(A \cap B).$$

c. A sample of 100 dry battery cells tested to find the length of life produced the following results $\bar{x} = 12$ hours, $s = 3$ hours, Assuming that the data are normally distributed, what percentage of batter cells are expected to have life (i) more than 15 hours, (ii) Less than 6 hours and (iii) between 10 and 14 hours.

d. (i) What are the different types of sampling?

(ii) Mention two important properties of Poisson distribution.

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